## **Some Precalculus Problems**

1. Express the area of a circle, A, in terms of its circumference, C.

2. Simplify:  $\sqrt[3]{\frac{-16x^3}{2y^6}}$ . 3. Perform the indicated operations and simplify:  $(m^{n+1}r^n)(3m^nr^{2n})^{-1}$ . 4. Perform the indicated operations and simplify:  $\frac{ab}{1+1}$ . 5. Find  $f^{-1}(x)$  for  $f(x) = \frac{1-3x}{4}$ . 6. Evaluate  $(5x+1)^{\frac{3}{4}} - (7-x)^0$  for x = 3. 7. Evaluate  $-(2b^2)^{-1}$  when b = -2. 8. Find the interval where g(x) > 0 if  $g(x) = -x^2 - x + 6$ . 9. If  $f(t) = \frac{2}{1-t}$ , for what value of t does f(t) = 3? 10. Simplify completely:  $2u(3u^2-1)-(-8u^3-14u+6)$ . 11. Simplify completely:  $4(2x+1)^2 + 3(2x+1) + 1$ . 12. Factor completely:  $32x^4y - 162y$ . 13. What is the remainder when  $5x^2 - 2x + 1$  is divided by x - 1? 14. Find a so that the two lines do not intersect: y = 4x + 2, y - 3 = ax. 15. Perform the indicated operation and simplify:  $\frac{4m^2 - v^2}{3m - 1} \div \frac{2m^2 + mv}{3m - 1}$ . 16. Perform the indicated operation and simplify:  $\frac{3c}{c-2} + \frac{c+1}{2-c}$ . 17. Simplify completely:  $\frac{\frac{a}{x} - \frac{x}{a}}{1 - 1}$ 18. Solve for z: 7z - (4z - 9) = 24 + 5(z - 1). 19. Solve for  $x: \frac{a}{3} + 5x = b\left(\frac{x}{3} + 2\right)$ . 20. Solve for  $r: S = \frac{2r-a}{r-1}$ . 21. Solve for  $R: V = \frac{3R}{a} - \frac{R}{b}$ . 22. Solve for  $t: 2t^2 + 4t = 9t + 18$ . 23. Solve for  $s: -2s^2 - 4s + 2s^3 = 0$ .

- 24. Solve for  $m: m^3 + 3m^2 4m 12 = 0$ .
- 25. Solve for  $p: \frac{4}{p} \frac{2}{p+1} = 3$ .
- 26. To get a B in a course a student must have an average of at least 80% on five tests that are worth 100 points each. On the first four tests a student scores 92%, 83%, 61%, and 71%. Determine the lowest score the student can receive on the fifth test to assure a grade of B for the course.
- 27. The area of a rectangle is 84 square feet and the length is 6 feet longer than the width. If *w* represents the width, write an equation that could be used to find the dimensions of the rectangle.
- 28. A furniture store drops the price of a table 37 percent to a sale price of \$364.77. What is the original price?
- 29. The cost of mailing envelopes by bulk mail is \$35 for the first 200 plus \$0.12 for each additional envelope over 200. Write a function to represent the cost of mailing *x* envelopes when  $x \ge 200$ .
- 30. Solve for *t*:  $(t+2)^2 = 8$ .
- 31. Solve for y:  $-15y + 6y^2 = -y$ .
- 32. Solve for *z*:  $z^2 4z + 6 = 0$ .
- 33. If a solution to f(x) = 0 is x = 5, find a solution to 3f(x+2) = 0.
- 34. Solve for *x*:  $\sqrt{x+6} = x$
- 35. Solve for  $r: 5-3r \le 8$ .
- 36. Find the length of *b*:



- 37. Find the area of the triangle bounded by y = 5 2x, the *x*-axis, and the *y*-axis in the first quadrant.
- 38. Solve for *x*:  $|2x+1| \ge 7$ .
- 39. Find the domain of  $y = \sqrt{4-5x}$ .
- 40. Graph  $y = \frac{6}{r}$ .
- 41. Find the intercepts of  $y 2x^2 13x = 6$ .
- 42. Find the equation of the graph :



- 43. Find the distance between (6,3) and (-2,4).
- 44. Find the midpoint of the line segment joining (6,9) and (-3,1).
- 45. What is the range of  $y = 2(3)^t$ ?
- 46. Find the equation of the line perpendicular to 3y+2x-3=0 passing through (4,-1).

- 47. Find f(-4) if  $f(x) = \frac{2x^2 11}{3x}$ . 48. Find f(b+2) if f(x) = 5 - 3(x+1). 49. Find the domain of  $g(x) = \frac{1}{x^2 - x - 12}$ . 50. Find h(3) if  $h(t) = \begin{cases} 2t^2 - 5 & t < -1 \\ 4 - 3t & t \ge -1 \end{cases}$ .
- 51. Find the domain and the range of the function:



- 52. If (5,6) is a point on the graph of y = g(x), find a point on the graph of y = -g(x) + 1.
- 53. Find g(f(-2)) if  $f(x) = \log_4(-8x)$  and g(x) = x 3.
- 54. If  $h(t) = \frac{t}{t+1}$ , find the value of t so that h(t) = 3.
- 55. If the graph of y = f(x) is below, sketch the graph of y = |f(x)|.



56. Sketch the graph of  $y = \log_3(x+2)$ .

57. Rewrite  $5^b = a$  in logarithmic form.

- 58. Rewrite as a single logarithm:  $\frac{1}{2}\log x + 4\log y 2\log z$ .
- 59. Solve for *t*:  $3^{2t} = 27^{2t-1}$ .
- 60. Solve for *r*:  $3 + 6e^{2r} = 5$ .
- 61. Solve for y:  $\log_3 y \log_3(y-1) = 2$ .
- 62. Solve the system of equations:  $\begin{cases} 4x + 3y = 0\\ 8x = 9y + 2 \end{cases}$

63. If  $f(x) = -x^2$  and g(x) = x + 4, find the values of x so that g(f(x)) > 0.

64. Express the length of side *a* in terms of *m*:



65. If  $\tan \theta = B$  where  $\theta$  is an angle in quadrant I, express  $\sin \theta$  in terms of B.

66. Find the trigonometric equation for this graph:



67. 
$$\sin(\theta + \pi) =$$

68. Find  $\cos\left(\frac{4\pi}{3}\right)$ .