## Some Precalculus Problems

1. Express the area of a circle, $A$, in terms of its circumference, $C$.
2. Simplify: $\sqrt[3]{\frac{-16 x^{3}}{2 y^{6}}}$.
3. Perform the indicated operations and simplify: $\left(m^{n+1} r^{n}\right)\left(3 m^{n} r^{2 n}\right)^{-1}$.
4. Perform the indicated operations and simplify: $\frac{a b}{\frac{1}{a}+\frac{1}{b}}$.
5. Find $f^{-1}(x)$ for $f(x)=\frac{1-3 x}{4}$.
6. Evaluate $(5 x+1)^{3 / 4}-(7-x)^{0}$ for $x=3$.
7. Evaluate $-\left(2 b^{2}\right)^{-1}$ when $b=-2$.
8. Find the interval where $g(x)>0$ if $g(x)=-x^{2}-x+6$.
9. If $f(t)=\frac{2}{1-t}$, for what value of $t$ does $f(t)=3$ ?
10. Simplify completely: $2 u\left(3 u^{2}-1\right)-\left(-8 u^{3}-14 u+6\right)$.
11. Simplify completely: $4(2 x+1)^{2}+3(2 x+1)+1$.
12. Factor completely: $32 x^{4} y-162 y$.
13. What is the remainder when $5 x^{2}-2 x+1$ is divided by $x-1$ ?
14. Find $a$ so that the two lines do not intersect: $y=4 x+2, y-3=a x$.
15. Perform the indicated operation and simplify: $\frac{4 m^{2}-v^{2}}{3 m-1} \div \frac{2 m^{2}+m v}{3 m-1}$.
16. Perform the indicated operation and simplify: $\frac{3 c}{c-2}+\frac{c+1}{2-c}$.
17. Simplify completely: $\frac{\frac{a}{x}-\frac{x}{a}}{\frac{1}{a}-\frac{1}{x}}$
18. Solve for $z: 7 z-(4 z-9)=24+5(z-1)$.
19. Solve for $x: \frac{a}{3}+5 x=b\left(\frac{x}{3}+2\right)$.
20. Solve for $r: S=\frac{2 r-a}{r-1}$.
21. Solve for $R: V=\frac{3 R}{a}-\frac{R}{b}$.
22. Solve for $t: 2 t^{2}+4 t=9 t+18$.
23. Solve for $s:-2 s^{2}-4 s+2 s^{3}=0$.
24. Solve for $m: m^{3}+3 m^{2}-4 m-12=0$.
25. Solve for $p: \frac{4}{p}-\frac{2}{p+1}=3$.
26. To get a B in a course a student must have an average of at least $80 \%$ on five tests that are worth 100 points each. On the first four tests a student scores $92 \%, 83 \%, 61 \%$, and $71 \%$. Determine the lowest score the student can receive on the fifth test to assure a grade of B for the course.
27. The area of a rectangle is 84 square feet and the length is 6 feet longer than the width. If $w$ represents the width, write an equation that could be used to find the dimensions of the rectangle.
28. A furniture store drops the price of a table 37 percent to a sale price of $\$ 364.77$. What is the original price?
29. The cost of mailing envelopes by bulk mail is $\$ 35$ for the first 200 plus $\$ 0.12$ for each additional envelope over 200. Write a function to represent the cost of mailing $x$ envelopes when $x \geq 200$.
30. Solve for $t:(t+2)^{2}=8$.
31. Solve for $y:-15 y+6 y^{2}=-y$.
32. Solve for $z: z^{2}-4 z+6=0$.
33. If a solution to $f(x)=0$ is $x=5$, find a solution to $3 f(x+2)=0$.
34. Solve for $x: \sqrt{x+6}=x$
35. Solve for $r: 5-3 r \leq 8$.
36. Find the length of $b$ :

37. Find the area of the triangle bounded by $y=5-2 x$, the $x$-axis, and the $y$-axis in the first quadrant.
38. Solve for $x:|2 x+1| \geq 7$.
39. Find the domain of $y=\sqrt{4-5 x}$.
40. Graph $y=\frac{6}{x}$.
41. Find the intercepts of $y-2 x^{2}-13 x=6$.
42. Find the equation of the graph :


43 . Find the distance between $(6,3)$ and $(-2,4)$.
44 . Find the midpoint of the line segment joining $(6,9)$ and $(-3,1)$.
45. What is the range of $y=2(3)^{t}$ ?
46. Find the equation of the line perpendicular to $3 y+2 x-3=0$ passing through $(4,-1)$.
47. Find $f(-4)$ if $f(x)=\frac{2 x^{2}-11}{3 x}$.
48. Find $f(b+2)$ if $f(x)=5-3(x+1)$.
49. Find the domain of $g(x)=\frac{1}{x^{2}-x-12}$.
50. Find $h(3)$ if $h(t)=\left\{\begin{array}{ll}2 t^{2}-5 & t<-1 \\ 4-3 t & t \geq-1\end{array}\right.$.
51. Find the domain and the range of the function:

52. If $(5,6)$ is a point on the graph of $y=g(x)$, find a point on the graph of $y=-g(x)+1$.
53. Find $g(f(-2))$ if $f(x)=\log _{4}(-8 x)$ and $g(x)=x-3$.
54. If $h(t)=\frac{t}{t+1}$, find the value of $t$ so that $h(t)=3$.
55. If the graph of $y=f(x)$ is below, sketch the graph of $y=|f(x)|$.

56. Sketch the graph of $y=\log _{3}(x+2)$.
57. Rewrite $5^{b}=a$ in logarithmic form.
58. Rewrite as a single logarithm: $\frac{1}{2} \log x+4 \log y-2 \log z$.
59. Solve for $t: 3^{2 t}=27^{2 t-1}$.
60. Solve for $r: 3+6 e^{2 r}=5$.
61. Solve for $y: \log _{3} y-\log _{3}(y-1)=2$.
62. Solve the system of equations: $\left\{\begin{array}{l}4 x+3 y=0 \\ 8 x=9 y+2\end{array}\right.$.
63. If $f(x)=-x^{2}$ and $g(x)=x+4$, find the values of $x$ so that $g(f(x))>0$.
64. Express the length of side $a$ in terms of $m$ :

65. If $\tan \theta=B$ where $\theta$ is an angle in quadrant I , express $\sin \theta$ in terms of $B$.
66. Find the trigonometric equation for this graph:

67. $\sin (\theta+\pi)=$
68. Find $\cos \left(\frac{4 \pi}{3}\right)$.

